

# Towards a Cooperative Defense Model Against Network Security Attacks

Harikrishna<sup>1</sup>, Venkatanathan<sup>1</sup> and Pandu Rangan<sup>2</sup>

<sup>1</sup>College of Engineering Guindy, Anna University Chennai, Tamil Nadu, India

<sup>2</sup>Indian Institute of Technology, Madras, Tamil Nadu, India

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Motivation

- People invest in security only if the loss due to a security attack is sufficiently high.
- Individuals who do not secure themselves become vulnerabilities for everyone else in a network.
- Users who desperately need security will contribute to the cost of protection of unprotected network users

# Motivation

- People invest in security only if the loss due to a security attack is sufficiently high.
- Individuals who do not secure themselves become vulnerabilities for everyone else in a network.
- Users who desperately need security will contribute to the cost of protection of unprotected network users

Is cooperation possible to assure better security? How?

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Related Work

## Security Games

A game-theoretic model that captures the essentials of decision making to protect and self-insure resources within a network.

- First proposed by Varian (2002) and extended by Grossklags et al. (2008).
- Grossklags et al. consider two types of security investments:
  - Self-protection: e.g. firewalls & IDS.
  - Self-insurance: e.g. backup technologies.
- The model has also been extended with heterogeneous players and incomplete information.
- All existing models assume that the players are **non-cooperative**.

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution**
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Our Contribution

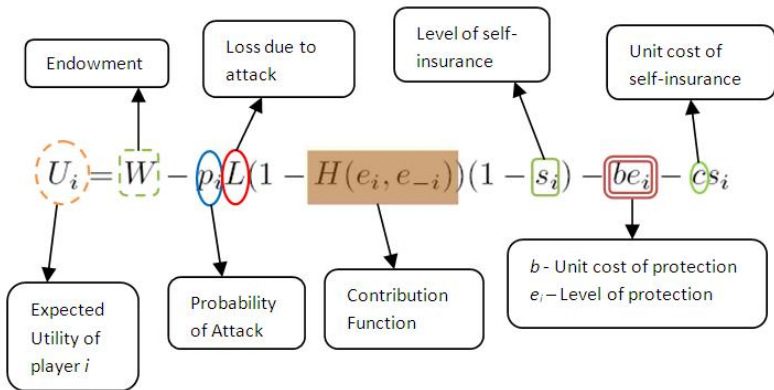
- We introduce the notion of **'joint protection'**, where one or more users subsidize the protection efforts of other users.
- We also introduce heterogeneity in **player attitude** in the form of pessimism and optimism.
- Using Cooperative Game Theory, we model security games as **Partition Function Games (PFGs)**.



# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games**
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Grossklag's Utility Function



# Contribution Functions

- The contribution function  $H$  characterizes the effect of a player's protection level, subject to the protection level of other players.

- **Weakest Link Game:**  $H(e_i, e_{-i}) = \min(e_i, e_{-i})$

Example: Weak passwords in a network.

- **Total Effort Game:**  $H(e_i, e_{-i}) = \frac{1}{n} \sum_{k=1}^n e_k$

Example: In distributed file transfer services, an attacker's motive is to slow down the rate of file transfer.

- **Best Shot Game:**  $H(e_i, e_{-i}) = \max(e_i, e_{-i})$

Example: To censor a piece of information, attacker has to ensure that no single copy of the information is available in the network.

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model**
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Types of Defenders

## Active Player:

- Have an incentive to protect themselves.
- Expected loss due to attack is  $L_a$ .
- Protection is cheaper for him when compared to the expected loss due to an attack and the insurance cost.

$$b = \min(L_a, b, c)$$

## Passive Player:

- Have no incentive to protect themselves and remain passive.
- Expected loss due to attack is  $L_p$ .
- Passivity is cheaper than self-protection and self-insurance.

$$L_p = \min(L_p, b, c)$$

**Assumption:** Self-insurance is more expensive than self-protection ( $c > b$ ).

# Need For Cooperation

- Full protection is a social optimum, but is difficult to achieve when players are competitive.
- In the weakest-link and total effort games, **full protection is not possible even if a single player is passive.**
- In the best shot game, **full protection is possible only if one player protects, while all other free ride on him.**
- In cases where competition fails, can full protection be achieved through cooperation?

# Cooperative Model

- The three canonical security games are modeled as coalitional games.
- We define **cooperation** as **the willingness of players to form a coalition and contribute to the cost of protection of the entire coalition.**
- In a coalition, active players contribute to the cost of protection of the passive players.
- A **value** is associated with each coalition, which is shared among the coalitional members.

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries**
  - **Partition Function Games (PFGs)**
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions



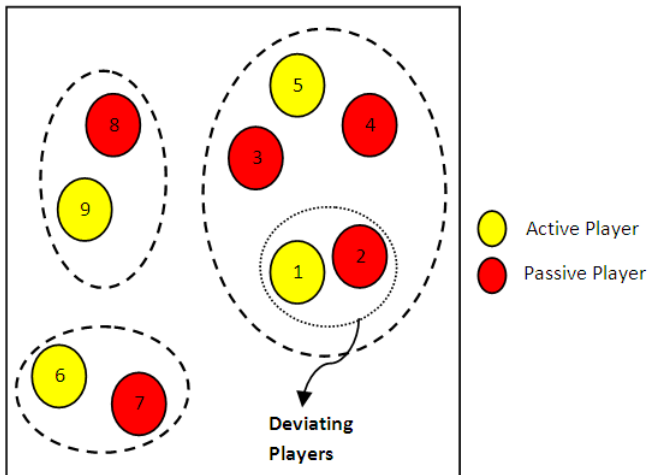
# Partition Function Games (PFGs)

**We utilize PFGs to design the cooperative model for the three canonical security games.**

- Introduced by Thrall and Lucas (1963) to model coalition formation with **externalities**.
- Given a set of players  $N$ , any non-empty subset of players is a **coalition**.
- A **partition**  $\mathcal{P}$  is a set of disjoint coalitions whose union is  $N$ .
- We denote the value assigned to a coalition  $P$  in partition  $\mathcal{P}$  as  $V(P, \mathcal{P})$ .
- Each player is *allocated a part of his coalition's value* called **payoff**.

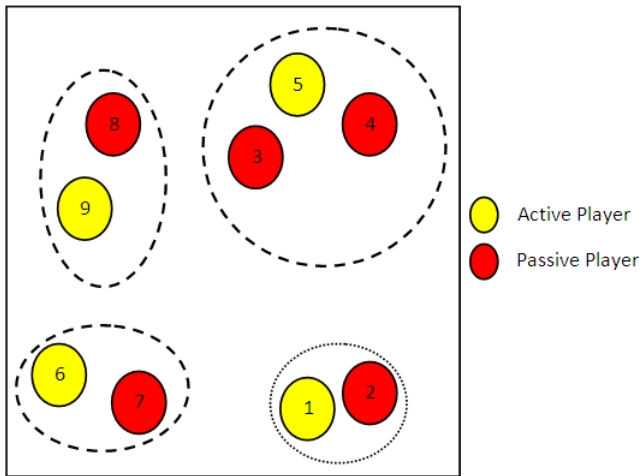
# Deviation

- Given a partitioning of players, a set of players may choose to deviate from the current setup.



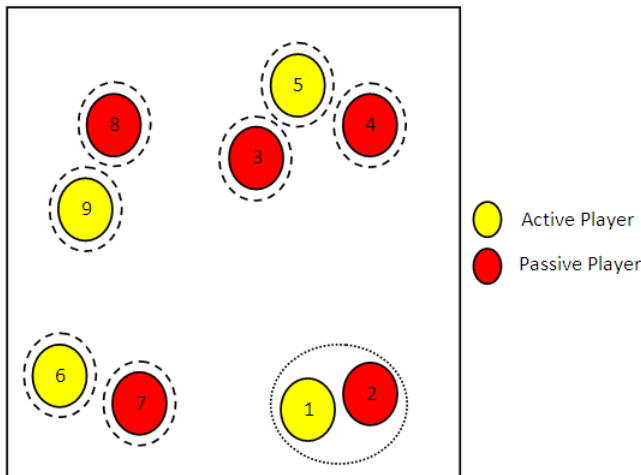
# Optimism

- If the players are **optimistic**, they expect the **best** possible outcome after deviation.



# Pessimism

- If the players are **pessimistic**, they expect the **worst** possible outcome after deviation.



# Core

## Core

The core is a set of partitioning of players along with their allocated payoffs, where no player has an incentive to deviate.

- The **success of cooperation** in a security game depends on the **non-emptiness of the core**.
- Two types of core.
  - Optimistic Core:** Assumes optimistic player attitude.
  - Pessimistic Core:** Assumes pessimistic player attitude.
- It can be shown that in a security game, a non-empty core would contain an outcome with the **grand coalition** of all players.

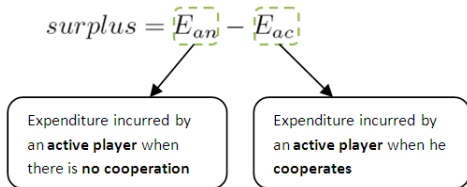
# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games**
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions

# Notion of Surplus and Deficit

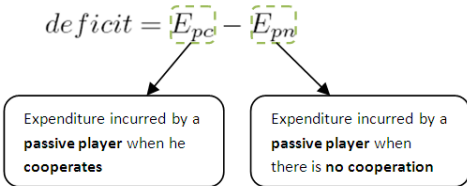
- **Surplus** is the maximum contribution of an active player towards the protection of passive players in the coalition.

$$surplus = E_{an} - E_{ac}$$



- **Deficit** is the additional amount of money that a passive player requires if he needs to engage in full protection.

$$deficit = E_{pc} - E_{pn}$$



# Weakest-link Game

- Consider a coalition  $P$  with  $l$  active players and  $k$  passive players. If every player outside  $P$  is protected,

$$V(P, \mathcal{P}) = l \times \textit{surplus} - k \times \textit{deficit}$$

- For a weakest-link game,

$$\textit{surplus} = L_a - b = \alpha(\textit{say})$$

$$\textit{deficit} = b - L_p = \beta(\textit{say})$$

- Then,

$$V(P, \mathcal{P}) = l\alpha - k\beta$$



## Weakest-link Game: Pessimistic Core

**Result:** *The pessimistic core of a weakest-link security game with  $n_a$  active players and  $n_p$  passive players is non-empty if and only if*

$$n_a\alpha - n_p\beta \geq 0$$

Full protection is thus possible if:

- Players are **pessimistic**.
- The expected loss due to an attack for active players is **sufficiently high** that they prefer cooperation over non-cooperation.

# Weakest-link Game: Optimistic Core

**Result:** *The optimistic core of a weakest-link security game with  $n_a$  active players and  $n_p$  passive players is non-empty if and only if*

- 1  $n_a\alpha - n_p\beta \geq 0$  and
- 2 **there exists no values** of  $0 \leq l \leq n_a$  and  $0 \leq k \leq n_p$  such that

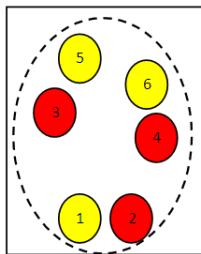
$$\frac{k}{l} \neq \frac{n_p}{n_a}$$

and  $0 \leq l\alpha - k\beta \leq n_a\alpha - n_p\beta$ .

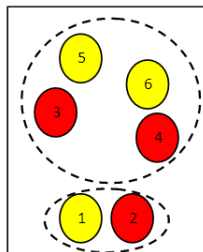
# Weakest-link Game: Optimistic Core (Continued)

When players are optimistic, full protection is possible if **one** of the following holds.

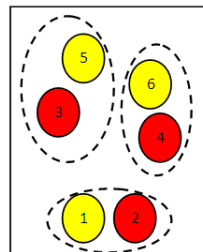
- The **grand coalition is the only formation**, where all passive players can be protected.
- There exists **multiple coalition structures** where all passive players are protected, but the **ratio between the number of passive and active players** in all the coalitions is equal to  $\frac{n_p}{n_a}$ .



Grand Coalition



Multiple Coalition Structures (with ratio constraint)



# Total Effort Game

- When there are  $n$  players, a player is assured of only  $\frac{1}{n}$ <sup>th</sup> of **his protection efforts**.
- A player self-protects only when his loss due to an attack is at least as high as  $n$  times the cost of protection.
- We assume that  $L_a \geq nb$  for an active player and  $L_p < b$  for a passive player.
- Here, we get

$$V(P, \mathcal{P}) = (k + r)(l\alpha' + k\beta') - kb,$$

where  $\alpha' = \frac{L_a}{n}$  and  $\beta' = \frac{L_p}{n}$

# Core in a Total Effort Game

## Results:

- The **pessimistic core** of a total effort game with  $n_a$  active players and  $n_p$  passive players is non-empty.
- The **optimistic core** of a total effort game is non-empty if and only if there is exactly one active player in the game.

Full protection is possible in a total effort game when **one** of the following holds.

- The players are optimistic, but there is **exactly one** active player in the network.
- The players are pessimistic, but there is **at least one** active player in the network.

# Best Shot Game

- We define cooperation slightly different:

**The players take turns and protect themselves**

(or)

**A single player is self-protected throughout, while every one shares the cost of protection**

- As long as a single active player is protected, passive players have no effect on the overall protection level and are not considered.
- Here,

$$V(P, \mathcal{P}) = IW - b$$

# Core in a Best Shot Game

## Results:

- *The **pessimistic core** of a best shot game with more than one active player is non-empty.*
- *The **optimistic core** of a best shot game with more than one active player is empty.*

Full protection is possible when **one** of the following holds true.

- There is **only one** active player in the network.
- There is **more than one** active player in the network, but all players are pessimistic.

# Outline

- 1 Motivation
- 2 Related Work
- 3 Our Contribution
- 4 Security Games
  - Grossklag's Utility Function
  - Contribution Functions
- 5 Our Model
  - Types of Defenders
  - Cooperative Model
- 6 Preliminaries
  - Partition Function Games (PFGs)
- 7 Cooperative Security Games
  - Weakest-link Game
  - Total Effort Game
  - Best Shot Game
- 8 Conclusions



# Conclusions

- Full protection is difficult when the network contains one or more passive players. In such cases, the **players are better off cooperating** rather than competing.
- The success of joint protection efforts depends on the **attitude of the players** and the nature of the attack.
- In general, when the players are **optimistic** and the **network is large**, full protection becomes difficult to achieve.

# References

- 1 Robert M. Thrall and William F. Lucas. n-person games in partition function form. *Research Logistics Quarterly*, 10(1):281–298, 1963.
- 2 Hal R. Varian. System reliability and free riding. In *the First Workshop on Economics of Information Security*, University of California, Berkeley, May 2002.
- 3 Jens Grossklags, Nicolas Christin, and John Chuang. Secure or insure? a game-theoretic analysis of information security games. In *Proceedings of the 17th International World Wide Web Conference (WWW '08)*, Beijing, China, April 2008, pages 209–218.

## References (Contd.)

- 4 Jens Grossklags, Nicolas Christin, and John Chuang. Security and insurance management in networks with heterogeneous agents. In *Proceedings of the 9th ACM Conference on Electronic Commerce (EC '08)*, Chicago, IL, USA, July 2008, pages 160–169.
- 5 László A. Kóczy. The core of a partition function game. Technical report, KUL Centre for Economic Studies, Working Paper No. 25, November 2000.